

C_03 Key to More Chapter 1 Practice

Friday, January 13, 2017 3:02 PM

6. For each part below, describe how the graph of the second function compares to the graph of the first function:

a) $y = x^5$

$y = 3x^5$ VS by 3
 or $y = 3(x^5)$

b) $y = x^2$

$y = (4x)^2$ HS by $\frac{1}{4}$

c) $y = |x|$

$y = \left|\frac{1}{2}x\right|$ HS 2

d) $y = \frac{1}{x}$

$4y = \frac{1}{x}$ VS $\frac{1}{4}$

7. The function $y = f(x)$ is transformed to $3y = f(x)$. If the point $(-12, 12)$ lies on the graph of $y = f(x)$, what is its **image point** on the graph of $3y = f(x)$?

VS $\frac{1}{3}$ $(-12, 4)$

8. The function $y = f(x)$ is transformed to $y = f\left(-\frac{1}{2}x\right)$. If the point $(-2, 4)$ lies on the

graph of $y = f(x)$, what is its **image point** on the graph of $y = f\left(-\frac{1}{2}x\right)$?

$(-2, 4) \xrightarrow{\text{reflect across } y} (2, 4)$ HS by 2 $(4, 4)$ HS by -2
 (OR: HS by 2, reflect across y-axis)

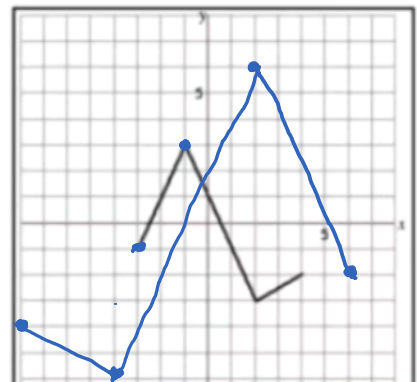
9a) List each change that will happen in the graph, when the equation $y = f(x)$ is

changed to $y = 2f\left(-\frac{1}{2}x\right)$. VS by 2
 HS by -2

b) The graph of $y = f(x)$ is shown on the grid. Sketch

the graph of $y = 2f\left(-\frac{1}{2}x\right)$ on the same grid.

ORIG	new
-3	-1
-1	3
2	-3
4	-2
6	-2
2	6
-4	-6
-8	-4



REVIEW OF 1.3-1.4, AND DOMAIN/RANGE

1. Suppose that the graph of $y = f(x)$ contains the point $(24, 4)$. Find the *image point* under each of the following transformations:

a) $y = -2f(3(x+2)) + 7$ b) $y = f(8(x-2)) + 2$

$(24, 4) \rightarrow (24, -4) \rightarrow (24, -8) \rightarrow (8, -8) \rightarrow \boxed{(6, -1)}$

a) $y = f(8(x-2)) + 2$ $(24, 4)$
 HS $\frac{1}{8}$ $\rightarrow (3, 4)$
 right 2 $\rightarrow (5, 4)$
 up 2 $\rightarrow \boxed{(5, 6)}$

2. A function, $y = g(x)$, has domain $\{x \mid 5 \leq x \leq 9, x \in \mathbb{R}\}$ and range $\{y \mid -4 \leq y \leq 12, y \in \mathbb{R}\}$.

- a) What is the domain of the inverse of $g(x)$?
 $\{x \mid -4 \leq x \leq 12, x \in \mathbb{R}\}$
- b) What is the range of the inverse of $g(x)$?
 $\{y \mid 5 \leq y \leq 9, y \in \mathbb{R}\}$

3. State the domain for each of the following. Remember that division by zero is undefined and that we cannot take square roots of negative numbers – this should help you figure out the domains.

a) $f(x) = \frac{5}{x-3}$

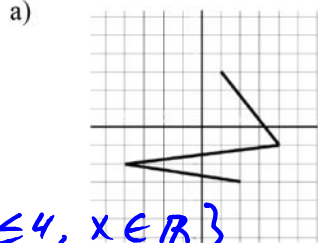
$x-3 \neq 0$
 $x \neq 3$

$\{x \mid x \neq 3, x \in \mathbb{R}\}$

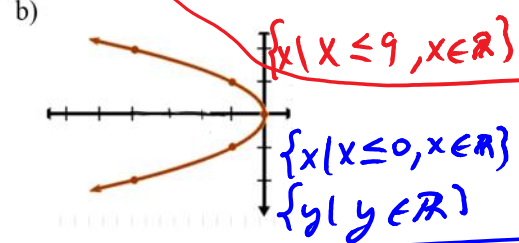
b) $f(x) = \sqrt{18-2x}$

$18-2x \geq 0$
 $\frac{18}{2} \geq \frac{2x}{2}$
 $9 \geq x$

4. State the domain and range for each of the following:



$\{x \mid -4 \leq x \leq 4, x \in \mathbb{R}\}$
 $\{y \mid -3 \leq y \leq 3, y \in \mathbb{R}\}$



5. What is the equation of the inverse of $f(x) = 3x + 12$?

- 1) replace $f(x)$ with y : $y = 3x + 12$
- 2) trade x and y : $x = 3y + 12$

$x = 3y + 12$

$\frac{x-12}{3} = \frac{3y}{3}$

$y = \frac{x-12}{3}$ } solve for y .

- 1a) $(6, -1)$ b) $(5, 6)$
- 2a) $\{x \mid -4 \leq x \leq 12, x \in \mathbb{R}\}$ b) $\{y \mid 5 \leq y \leq 9, y \in \mathbb{R}\}$
- 3a) $\{x \mid x \neq 3, x \in \mathbb{R}\}$ b) $\{x \mid x \leq 9, x \in \mathbb{R}\}$
- 4a) $\{x \mid -4 \leq x \leq 4, x \in \mathbb{R}\}$ $\{y \mid -3 \leq y \leq 3, y \in \mathbb{R}\}$
- b) $\{x \mid x \leq 0, x \in \mathbb{R}\}$ $\{y \mid y \in \mathbb{R}\}$

5. $y = \frac{x-12}{3}$, or $f^{-1}(x) = \frac{x-12}{3}$

$f^{-1}(x) = \frac{x-12}{3}$

PREC12 Chapter 1 Practice Test

Name: Answer Key

1. If y is replaced by $y + 3$ in a function, then the graph of the new function will be:

- A. translated up 3
- B. translated down 3
- C. vertically stretched, factor 3
- D. vertically stretched, factor $\frac{1}{3}$

2. The point $(3, 5)$ is on the graph of the function $y = f(x)$. The point $(0, 6)$ is on the graph of the function $y = f(x - a) + b$. What are the values of a and b ?

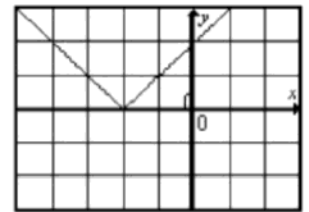
- A. $a = 3, b = 1$
- B. $a = 3, b = -1$
- C. $a = -3, b = 1$
- D. $a = -3, b = -1$

Point has moved 3 left and 1 up, so we have $y = f(x + 3) + 1$ which means the same thing as $y = f(x - (-3)) + 1$

3. Which equation will move the graph of $y = x^2$ three units to the left?

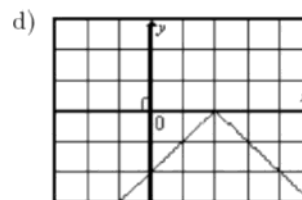
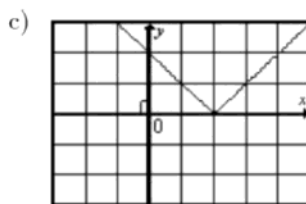
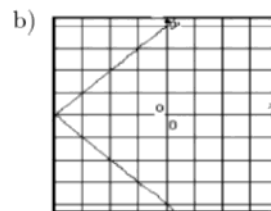
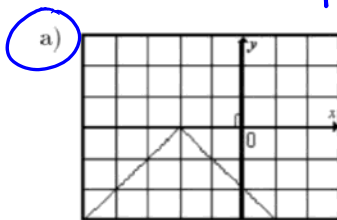
- A. $y - 3 = x^2$
- B. $y = x^2 - 3$
- C. $y = (x - 3)^2$
- D. $y = (x + 3)^2$

4. The graph of $y = g(x)$ is given at right.



A graph of $y = -g(x)$ would appear as which graph below?

reflect across the y-axis
(upside-down)



5. In which line is $y = 2x^2 - 3x$ reflected to obtain $x = 2y^2 - 3y$?

- A. $y = x$
- B. x -axis
- C. y -axis
- D. both x -axis and y -axis

x 's and y 's have interchanged,
so reflects across $y = x$

This reflects across the y-axis,
so the "mirror" is the y-axis.

6. If $y = f(x)$ is transformed to $y = f(-x)$, any **invariant points** will lie on:

- A. the x-axis
 B. the y-axis
 C. the line $y = x$
 D. there are no invariant points

7. The point $(7, -4)$ is on the graph of the function $y = f(x)$. Which point must be on the graph of the function $y = -2f(x)$? *NS by 2 and reflect across x-axis => multiply y-coordinate by -2.*

- A. $(7, -8)$
 B. $(7, 8)$
 C. $(7, -2)$
 D. $(7, 2)$

8. What value of a in the equation $y = \sqrt{ax}$ will cause a horizontal stretch, factor $\frac{1}{3}$?

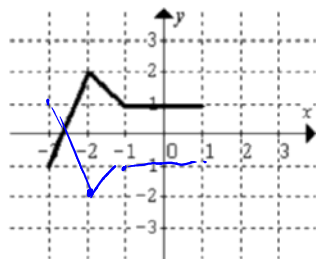
- A. $a = \frac{1}{3}$
 B. $a = 3$
 C. $a = -\frac{1}{3}$
 D. $a = -3$

9. If $y = f(x)$ is compared to $y = f(3x - 6)$, what transformations have occurred?

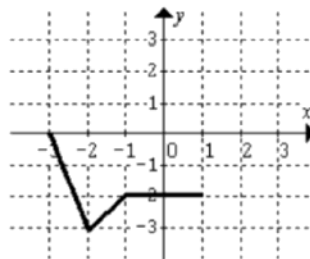
- A. horizontal stretch factor $\frac{1}{3}$, right 6 units
 B. horizontal stretch factor $\frac{1}{3}$, right 2 units
 C. horizontal stretch factor 3, right 2 units
 D. horizontal stretch factor 3, right 6 units

Factor first:
 $y = f(3(x-2))$
 \Rightarrow $\left[\begin{array}{l} \text{HS by } \frac{1}{3} \\ \text{2 units right} \end{array} \right.$

10. The graph of $y = f(x)$ is given below. What transformations will produce the new image?



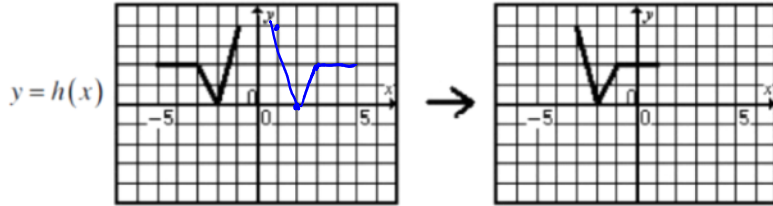
?



- A. reflect in the x-axis and shift down one
 B. reflect in the x-axis and shift up one
 C. reflect in the y-axis and shift down one
 D. reflect in the y-axis and shift up one

it's upside-down, so
 reflect across x-axis
 then
 shift down 1 unit

11. The graph of $y = h(x)$ is shown below. What new equation will produce the graph of the transformed function?



reflect in the y-axis
then
shift 4 units
left

- A. $-y = h(x+4)$ B. $y = h(-x)$
 C. $y = h(-(x+4))$ D. $y = h(-(x-4))$

12. The point (a, b) is on the graph of $y = f(x)$. Which point must be on the graph of $y + 2 = 3f(-x)$?

- A. $(-a, 3b-2)$ B. $(-a, 3(b-2))$
 C. $(-a, \frac{b-2}{3})$ D. $(-a, \frac{b}{3}-2)$

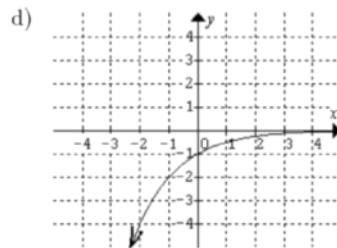
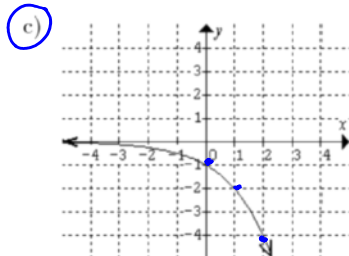
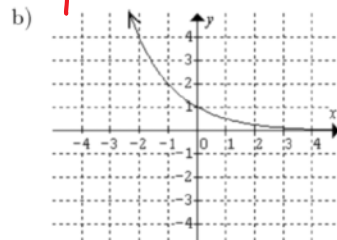
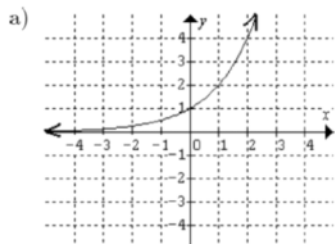
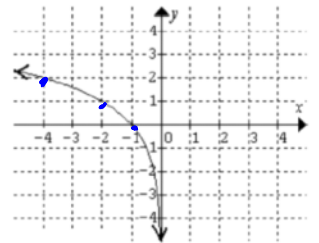
$y = 3f(-x) - 2$
 ↓ vs 3 ↓ reflect across y-axis ↓ down 2

13. Identify the graph of the inverse for the function shown at right.

trade x and y coordinates

ORIG
 $\begin{array}{r|l} -4 & 2 \\ -2 & 1 \\ -1 & 0 \end{array}$

inverse
 $\begin{array}{r|l} 2 & -4 \\ 1 & -2 \\ 0 & -1 \end{array}$



$y = x^3 + 4$

3...

inverse

14. Find $y = f^{-1}(x)$ if $f(x) = x^3 + 4$.

A. $f^{-1}(x) = x^3 - 4$

$y = x^3 + 4$

1) trade x and y: $x = y^3 + 4$

2) solve for y: $x - 4 = y^3$

$\sqrt[3]{x-4} = \sqrt[3]{y^3}$
 $\sqrt[3]{x-4} = y$

B. $f^{-1}(x) = \frac{1}{x^3 + 4}$

C. $f^{-1}(x) = \sqrt[3]{x} - 4$

D $f^{-1}(x) = \sqrt[3]{x-4}$

15. Calvin is asked what steps would be required to graph $y = f(2x+6)$ if he is given the graph of $y = f(x)$. He writes that the function needs to be vertically stretched by a factor of $\frac{1}{2}$ and then translated right 6 units. What mistakes did he make?

1) First, he should factor, to get $y = f(2(x+3))$

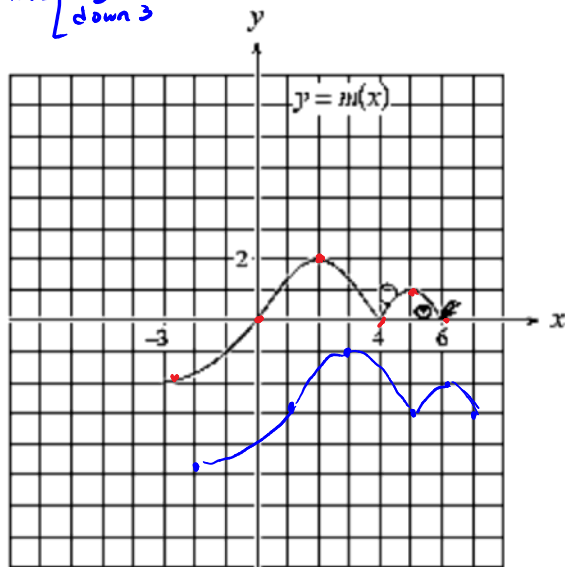
2) He should say horizontal stretch by $\frac{1}{2}$, and a translation LEFT, 3 units.

16. Omitted

17. Given the graph of $y = m(x)$ below,

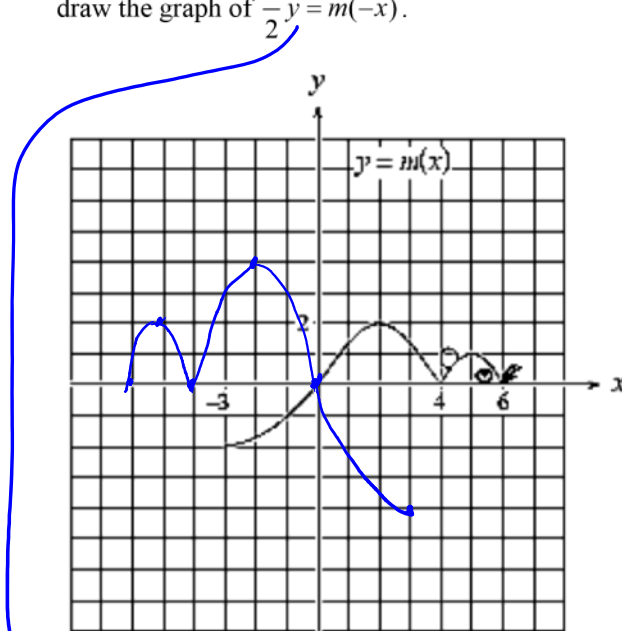
draw the graph of $y + 3 = m(x-1)$.

move right 1
down 3



18. Given the graph of $y = m(x)$ below,

draw the graph of $\frac{1}{2}y = m(-x)$.



ORIG	new
-3	-4
0	0
2	4
4	0
5	2
6	0

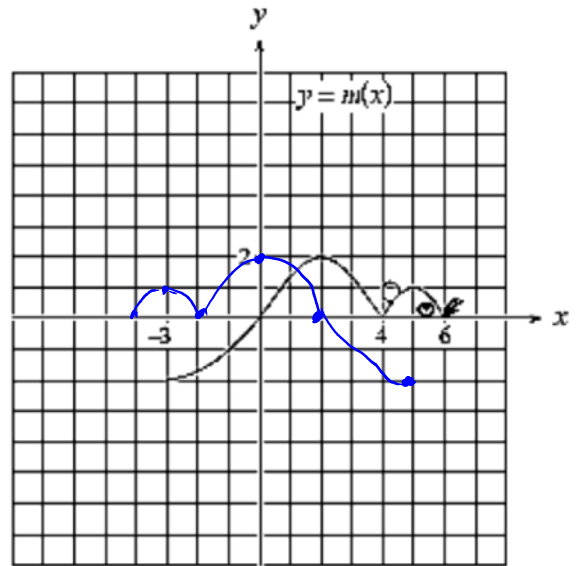
$\frac{1}{2}y = m(-x)$
means the same as

$\frac{2}{1}(\frac{1}{2}y) = \frac{2}{1}m(-x)$
 $y = 2m(-x)$

19. Given the graph of $y = m(x)$ at right, draw the graph of $y = m(-x+2)$.

Factor first: $y = m(-x+2)$
 $y = m(-1(x-2))$
 \Rightarrow reflect across y -axis
 translate 2 right

final pts	
5	-2
2	0
0	2
-2	0
-3	1
-4	0



20. Given the function $y = (x-3)^2 - 2$

a) Graph the function on the grid.
 b) Determine the domain of this function.

parabola,
 $V = (3, -2)$

$$\{x \mid x \in \mathbb{R}\}$$

c) Determine the range of this function.

$$\{y \mid y \geq -2, y \in \mathbb{R}\}$$

d) Graph the *inverse* of this function.

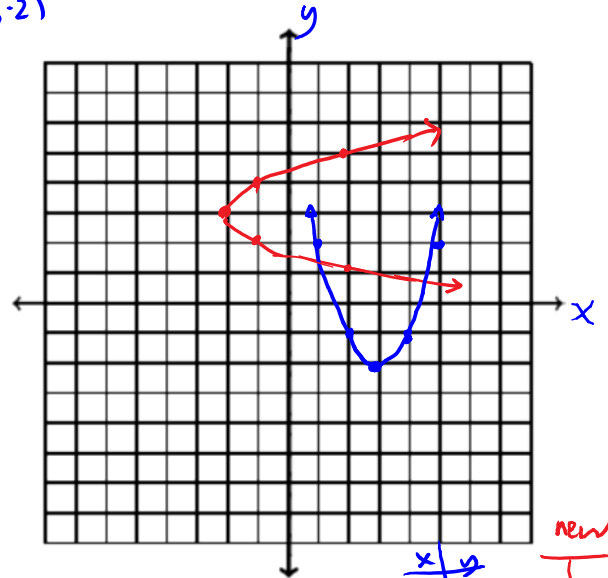
Trade x and y . (red graph)

e) How could you restrict the domain of

$y = (x-3)^2 - 2$ so that its inverse will also be a function?

Restrict domain to either $x \geq 3$, the right half of the parabola
 OR, to $x \leq 3$, the left half of the parabola

f) Algebraically, determine the equation of the inverse of $y = (x-3)^2 - 2$.



x	y	new
3	-2	-2
4	-1	-1
2	-1	-1
5	2	2
1	2	2

1) Trade x and y : $y = (x-3)^2 - 2$ becomes $x = (y-3)^2 - 2$
 2) Solve for y .

$$x+2 = (y-3)^2$$

$$\pm \sqrt{x+2} = \sqrt{(y-3)^2}$$

$$\pm \sqrt{x+2} = y-3$$

$$y = 3 \pm \sqrt{x+2}$$

To be a function, pick either

$$y = 3 + \sqrt{x+2} \quad (\text{top half}) \quad \rightarrow$$

To be a function, pick either

$$y = 3 + \sqrt{x+2} \quad (\text{top half})$$

$$y = 3 - \sqrt{x+2} \quad (\text{bottom half})$$



OR

